

# Pythagorean Triples



## Objective

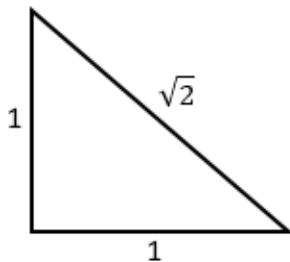
Print this worksheet to complete the activity. By completing this worksheet, you will be able to use the Pythagorean theorem to identify Pythagorean triples.

## The Pythagorean Theorem



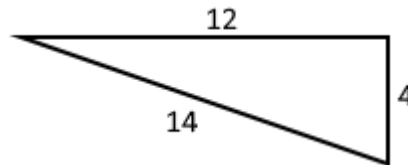
The **Pythagorean theorem** states that for a right triangle, the sum of the squares of the legs is equal to the square of the hypotenuse. In other words, if a right triangle has legs with side lengths of  $a$  and  $b$  and a hypotenuse with side length of  $c$ , then  $a^2 + b^2 = c^2$ .

If the values  $a$ ,  $b$ , and  $c$  satisfy the Pythagorean theorem and are all positive integers, then they form a **Pythagorean triple**. We write the triple in the form  $(a, b, c)$ . The three values are listed in order from least to greatest so that the last value is always the hypotenuse.



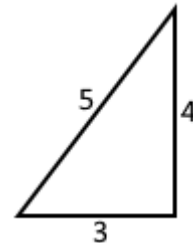
$$\begin{aligned}1^2 + 1^2 &= (\sqrt{2})^2 \\1 + 1 &= 2 \\2 &= 2\end{aligned}$$

These lengths satisfy the Pythagorean theorem but are not all integers, so they do not form a Pythagorean triple.



$$\begin{aligned}4^2 + 12^2 &= 14^2 \\16 + 144 &= 196 \\160 &\neq 196\end{aligned}$$

These lengths do not satisfy the Pythagorean theorem, so the triangle is not a right triangle.



$$\begin{aligned}3^2 + 4^2 &= 5^2 \\9 + 16 &= 25 \\25 &= 25\end{aligned}$$

These lengths satisfy the Pythagorean theorem and are all positive integers, so  $(3, 4, 5)$  forms a Pythagorean triple.

## ? Question

Use the Pythagorean theorem to determine whether each set of values forms a Pythagorean triple.

1.  $(8, 15, 17)$  \_\_\_\_\_

3.  $(9, 12, 16)$  \_\_\_\_\_

5.  $(20, 21, 29)$  \_\_\_\_\_

2.  $(1, \sqrt{3}, 2)$  \_\_\_\_\_

4.  $(8, 11, 14)$  \_\_\_\_\_

6.  $(30, 40, 50)$  \_\_\_\_\_